Growth and identities of semigroups of matrices

Jan Okniński, University of Warsaw, Poland

Finitely generated subsemigroups $S \subseteq M_n(K)$ of the multiplicative monoid of $n \times n$ matrices over a field K are considered. If $S = \langle a_1, \ldots, a_n \rangle$, then the corresponding growth function is defined by d(n) = the number of elements of Sthat can be presented as words of length at most n in the generators a_1, \ldots, a_n . Classical results on the growth of groups and partial results on the growth of semigroups of matrices will be presented. Connections between the growth rate of S, the identities satisfied in S and the structure of S will be discussed.